## UNIT 1 <br> Narmber System Fluency

## Essential Question

HOW can mathematical ideas be represented?


## Chaptery <br> Compriewfi <br> Molfiotgiallubers

The standard algorithm used to multiply and divide whole numbers can be applied to operations with decimals. In this chapter, you will multiply and divide multi-digit decimals.

## Chapcere <br> Multiply and Divide Fractions

Models and equations can be used to represent real-world situations involving operations with fractions. In this chapter, you will multiply and divide fractions by whole numbers and by fractions.

# Chapter 1 <br> Compute with Multi-Digit Wumbers 

Essential Question

HOW can estimating be helpful?

## CCGPS <br> Common Core GPS

Content Standards
MCC6.NS.2, MCC6.NS. 3
Mathematical Practices
1, 2, 3, 4, 5, 6

## Math in the Real World

Skyscrapers A certain skyscraper in Chicago has 1,200,000 square feet of space. On average, there are 29,268 square feet of space on each floor. Estimate to find the number of floors in the building.


## FOLDABLES

Cut out the correct Foldable from the FL pages in the back of this book.

Place your Foldable on the Key Concept page toward the end of this chapter.

Use the Foldable
throughout this chapter to help you learn about computing with multidigit numbers.

## Vocab <br> Vocabulary

compatible numbers

## Review Vocabulary

Graphic Organizer One way to remember vocabulary terms is to connect them to an everyday meaning or an example. Use this information to complete the graphic organizer.


## 



Common Core Review мсс4.лвт.5, мсс5.мвт. 6

## Example 1

Find $13 \times 15$.
13
15
$\times 65$
+130 Multiply the tens.
195

Multiply the ones.

Add.

## Example 2

Find $323 \div 17$.
$1 7 \longdiv { 1 9 }$
Divide the tens.
$-17$
Divide the ones.

## Quick Check

Multiply Find each product.

1. $15 \times 20=$ $\qquad$
2. $19 \times 51=$ $\qquad$
3. $49 \times 22=$ $\qquad$

Divide Find each quotient.
4. $112 \div 8=$ $\qquad$ 5. $539 \div 11=$
6. $779 \div 19=$
7. A musician sold 64 million albums in 16 months. She sold the same amount in each month. How many albums did she sell in each month?
(1)
(2)
(3)
(4) 5
(6) 7

6 Chapter 1 Compute with Multi-Digit Numbers

## Add and Subtract Decimals

## What You'll Learn

Scan the lesson. Predict two things you will learn about adding and subtracting decimals.

## Real-World Link

Swimming One event in competitive swimming is the women's 100-meter butterfly. The table shows the times of different swimmers at a recent Olympics.

| Women's 100-Meter Butterfly |  |  |
| :---: | :---: | :---: |
|  | Swimmer's | Time (s) |
|  | Lisbeth Trickett | 56.73 |
|  | Christine Magnuson | ? |
|  | Gabriella Silva | 58.10 |

## You can use place value charts to compare the results.

1. It took Christine Magnuson 0.37 second longer to finish than Lisbeth Trickett. What was Magnuson's time, in seconds?

2. At a high school meet, a swimmer swam the women's 100-meter butterfly in 72.34 seconds. How many seconds faster did Gabriella Silva swim her race?


## Add Decimals

To add decimals, line up the decimal points. Then, add digits in the same place-value position.

## Examples

Tutor

1. Find the sum of $\mathbf{2 3 . 1}$ and 5.8 .

Estimate $23.1+5.8 \approx 23+6$ or 29
23.1
$+5.8$
28.9

Line up the decimal points.

Add as with whole numbers.

Check for Reasonableness 28.9 $\approx 29$
The sum of 23.1 and 5.8 is 28.9.

## 2. Find the sum of 29.6 and 14.7.

Estimate $29.6+14.7 \approx \square+\square$ or $\square$


Line up the decimal points.

Add as with whole numbers.

Check for Reasonableness $\square$ $\approx$ $\square$
The sum of 29.6 and 14.7 is $\square$

Got It? Do these problems to find out.

## Find each sum.

a. $54.7+21.4$
b. $14.2+23.5$
c. $17.3+33.5$

8 Chapter 1 Compute with Multi-Digit Numbers

## Subtract Decimals

To subtract decimals, line up the decimal points. Then, subtract digits in the same place-value position. You may need to annex, or place zeros at the end of a decimal, in order to subtract.

## Examples

## 3. Find the difference of 5.774 and $\mathbf{2 . 3 7 1}$.

Estimate $\quad 5.774-2.371 \approx 6-2$ or 4
5.774 Line up the decimal points.
$-2.371$
3.403 Subtract as with whole numbers.

Check for Reasonableness $3.403 \approx 4 \checkmark$
So, $5.774-2.371=3.403$.

## 4. Find 6 - 4.78.

Estimate $6-4.78 \approx 6-5$ or 1
6.00 Annex zeros so that both numbers have the same number of decimal places.
$-4.78$
1.22

Check for Reasonableness $1.22 \approx 1 \checkmark$
So, $6-4.78=1.22$.
5. Find $23-4.216$.


Annex the zeros so that both numbers have
the same number of decimal places.

Subtract as with whole numbers.
So, $23-4.216=$ $\qquad$

Got It? Do these problems to find out.
Find each difference.
d. $9.543-3.671$
e. $\$ 50.62$ - $\$ 39.81$
f. $14-9.09$
. $14-9.09$

d. $\qquad$
e. $\qquad$
f. $\qquad$

## Example

6. Reagan is creating a video. The first video clip was 22.36 minutes long. The second video clip was 17.03 minutes long. What is the total length of the video?

Estimate $22.36+17.03 \approx 22+17$ or 39
22.36 Line up the decimal points.
$+17.03$
39.39 Add as with whole numbers.

Check for reasonableness $39.39 \approx 39 \boldsymbol{\checkmark}$
So, the video is 39.39 minutes long.

## Got It? Do this problem to find out.

g. Jonathan is traveling for work. This morning his GPS indicated that the total distance to his destination is 589.4 miles. Before lunch he drove 208.62 miles. How much farther does Jonathan need to travel?

## Guided Pregtice

Find each sum or difference. (Examples 1-5)

1. $14.7+87.9=$ $\qquad$ 2. $66.5-24.1=$ $\qquad$ 3. $52.1-31.47=$ $\qquad$

## Rate Yourself!

I understand how to add and subtract decimals.

Great! You're ready to move on!
$\square$ I still have questions about adding and subtracting decimals.

風 $N$ No Problem! Go online to access a Personal Tutor.


## Independent Practice

Find each sum. (Examples 1 and 2 )

1. $7.2+9.5=$ $\qquad$
2. $1.34+2=$ $\qquad$ $13.54 .5+48.51=$ $\qquad$

Find each difference. (Examples 3-5)
4. $5.6-3.5=$ $\qquad$
5. $97-16.98=$ $\qquad$ 6. $58.67-28.72=$ $\qquad$

17 The table shows the top three finishers in barrel racing. What is the time difference between Nicolas and Sancho?
(Example 6)

| Barrel Racing Results |  |
| :---: | :---: |
| Rider | Time (s) |
| Nicolas | 14.67 |
| Becki | 15.98 |
| Sancho | 16.40 |

8. In two months, Mica spent a total of $\$ 305.43$ on groceries. She spent $\$ 213.20$ in the first month. How much did she spend in the second month? (Example 6)
9. Financial Literacy A hat costs $\$ 10.95$ and a T-shirt costs $\$ 14.20$. How much change will you receive if you pay for both items with a $\$ 50$ bill?
10. CCGFS Use Math Tools The 4-by-100 meter relay is a track and field event involving four runners on each team.
a. What is the combined time of Carter and Frater?
b. How much faster did Powell run his leg of the race than Bolt?

| $\mathbf{4}$ by $\mathbf{1 0 0}$ Meter Times |  |
| :--- | :---: |
| Runner | Time (s) |
| Carter | 13.4 |
| Frater | 12 |
| Bolt | 12 |
| Powell | 11.7 |

c. What is the combined time of all the runners?

## H.O.T. Problems Higher Order Thinking

11. ccGrs Find the Error Luis is finding $8.9-3.72$. Find his mistake and correct it.
$\qquad$
$\qquad$
$\qquad$

12. cCGFS Reason Abstractly Write two different pairs of decimals whose sums are 14.1. One pair should involve regrouping.
13. Reason Inductively Explain how you know that the sum of 12.6, 3.1, and 5.4 is greater than 20.
14. CCGFS Persevere with Problems Josie found that $3.28+3.28+3.28=$ 9.84. What is the missing factor in the related multiplication problem
$3.28 \times \square=9.84$ ? Explain.
15. CCGSS Reason Abstractly Without subtracting 8.5 - 4.64, determine what digit will be in the hundredths place. Explain.

## Georgia Test Practice

16. Keira is buying items for her kitchen. The store sells a large mixing bowl for $\$ 12.95$, a spatula for $\$ 8.37$, and measuring cups for $\$ 9.99$. What is the total cost of these items?
(A) $\$ 21.32$
(B) $\$ 29.12$
(C) $\$ 31.31$
(D) $\$ 41.31$
$\qquad$

## ExtraPractice

Find each sum.

18. $0.796+13=$ $\qquad$ 19. $15.63+24.36=$
22. $14.39-12.16=$ $\qquad$
20. $19.86-4.94=$ $\qquad$ 21. $82-67.18=$ $\qquad$
23. Financial Literacy The current balance of Tami's checking account is $\$ 237.80$. Find the new balance after Tami writes a check for $\$ 29.95$.
24. The annual rainfall for Kayston Falls was 50.38 inches in 2012. In 2013, the annual rainfall was 55.76 inches. What is the difference in rainfall between the two years?
25. Sill The melting point of sodium is 97.8 degrees Celsius. The melting point of potassium is 63.65 degrees Celsius. How much higher is the melting point of sodium?
26. CCGTS Be Precise Collin needs three wooden boards to repair his porch. The lengths he needs are 2.2 meters, 2.82 meters, and 4.25 meters. He purchases a board that is 10 meters long and cuts the three sections. How much of the board that Collin purchased will be left?


## Georgia Test Practice

27. The table shows the top three finishers for a swimming event. What is the time difference between Kendrick and Andrew?

| Boy's $\mathbf{5 0}$ Yard Freestyle |  |
| :--- | :---: |
| Swimmer | Time (s) |
| Andrew | 22.63 |
| Kendrick | 22.20 |
| Ty | 22.58 |

(A) 0.38 s
(C) 44.83 s
(B) 0.43 s
(D) 45.08 s
28. Amaya has a store credit of $\$ 50.86$. She plans to purchase a video game for $\$ 24.97$ and a golf club accessory for $\$ 6.99$. How much store credit will she have left?
(F) $\$ 43.87$
(1) $\$ 25.89$
(G) $\$ 31.96$
(1) $\$ 18.90$
29. Short Response Dominic is traveling through the state of Oregon. He drove 66.4 miles from Salem to Eugene and then continued to Medford. The total distance of his trip was 233.25 miles. How far is the distance from Eugene to Medford?


## (CCGPS Common Core Review

Round each decimal to the nearest whole number. MCC5.NBT. 4
30. $4.75 \approx$
31. $34.1 \approx$ $\qquad$ 32. $22.48 \approx$
33. The table shows the distances Juliana biked several days this week. Which day of the week did she bike the greatest distance? mсс5.nвт.зb

| Day | Distance Biked (mi) |
| :--- | :---: |
| Monday | 9.34 |
| Wednesday | 9.47 |
| Thursday | 9.74 |
| Sunday | 9.32 |

34. Plot the number 2.78 on the number line below. mcc4.NF. 7


## Estimate Products

## What You'll Learn

Scan the lesson. List two real-world scenarios in which you would estimate products.
$\qquad$
-

## Real-World Link

Skateboarding The record for the greatest distance traveled on skateboard in 24 hours was set in a recent year by James Peters. He traveled about 7.6 miles per hour.

1. Plot 7.6 on the number line.

2. What whole number is 7.6 closest to?
3. Estimate how many miles James Peters traveled in 24 hours.
$\square$
$\qquad$
4. Is your estimate higher or lower than the actual distance he traveled? Explain.
$\qquad$
5. A new record was set later by Ted McDonald. He traveled about 10.1 miles per hour. About how much farther did Ted McDonald travel?


So, Ted McDonald traveled about $\qquad$ miles farther.

## Estimate Products Using Rounding

To estimate products of decimals, round each number. First underline the digit to be rounded. Then look at the digit to the right of the place being rounded.

- If the digit is 4 or less, the underlined digit remains the same.
- If the digit is 5 or greater, add 1 to the underlined digit.
- After rounding, all place values to the right of the underlined digit have a value of zero.

After the numbers are rounded, multiply.

## Examples

## Rounding Decimals

When rounding decimals, such as 99.96 to the tenths, the 9 must round up. So, 99.96 rounded to the nearest tenth is 100.0.
a. $\qquad$
b. $\qquad$
c. $\qquad$

1. Estimate $8.7 \times 2.8$.

Round to the nearest whole number to make it easier to compute mentally.

8.7 $\rightarrow$| 9 |
| :--- |
| $\times 2.8$ |$\rightarrow \frac{\text { Round } 8.7 \text { to } 9 .}{\times 3} \quad$ Round 2.8 to 3.

The product is about 27 .
2. Estimate $42.6 \times 37.2$.

Round to the greatest place value to make it easier to compute mentally.


The product is about $\qquad$ .

## Got It? Do these problems to find out.

Estimate each product.
a. $9.6 \times 1.8$
b. $4.2 \times 3.1$
c. $68.4 \times 21.3$

## Examples

3. A greyhound can travel 39.3 miles per hour. At this speed, about how far could a greyhound travel in 6.5 hours?

| 39.3 | $\rightarrow 40$ |
| ---: | :--- |
| $\times 6.5$ | $\rightarrow \frac{\text { Round } 39.3 \text { to } 40 .}{280}$ |$\quad$ Round 6.5 to 7.

The greyhound could travel about 280 miles in 6.5 hours.
4. Suppose one U.S. dollar is equal to 5.8 Egyptian pounds. About how many Egyptian pounds would you receive for $\mathbf{\$ 4 8 . 5 0}$ ?

Round to the greatest place value to make it easier to compute mentally.
$5.8 \approx$

$48.50 \approx$


So, $\$ 48.50$ is equal to about $\square$ Egyptian pounds.

Got It? Do these problems to find out.
d. SIIM Earth is rotating around the Sun about 18.6 miles per second. About how many miles does it travel in 4.8 seconds?
e. The average walking speed of a person is 4.8 kilometers per hour. Estimate the number of kilometers could you walk in 3 hours?
f. STIEM A King Palm can grow about 2.1 feet a year. Estimate the height of the King Palm, in yards, after 15 years.

You could estimate $18.76 \times 5$ by multiplying $19 \times 5$ or by multiplying $20 \times 5$. Which answer will be more exact? Explain below.
d. $\qquad$
e. $\qquad$
f. $\qquad$


## Example

5. Patrice has $\$ 20$ to buy 5 binders. Binders cost $\$ 4.29$ each. Does she have enough money? Explain your reasoning.

Estimate.
$5 \times \$ 4=\$ 20 \quad$ Estimate 4.29 as 4.
$5 \times \$ 5=\$ 25 \quad$ Estimate 4.29 as 5 .
The actual cost is between $\$ 20$ and $\$ 25$. So, Patrice does not have enough money to buy the binders.

## Eulded Practice

Estimate each product. (Examples 1 and 2)

1. $5.8 \times 4 \approx$ $\qquad$ 2. $13.92 \times 2.7 \approx$ $\qquad$ 3. $94.89 \times 3.11 \approx$
2. Financial Literacy A grocery store sells American cheese for $\$ 3.89$ per pound. About how much would 1.89 pounds of the cheese cost?
(Examples 3 and 4)
3. Greg has 52 megabytes left on his MP3 player. He wants to download 7 songs that each use 7.9 megabytes of memory. He estimates that he will need 56 megabytes of memory. Is his estimate is reasonable? Explain your reasoning. (Example 5)
$\qquad$
$\qquad$
4. Building on the Essential Question How do you determine which place value to use when estimating products?

Rate Yourself!
How confident are you about estimating products? Check the box that applies.


For more help, go online to access a Personal Tutor.

## Independent Practice

Estimate each product.
(Examples 1 and 2)

1. $9.7 \times 3.3 \approx$

2. $44.8 \times 5.1 \approx$
3. $3.4 \times 5.6 \approx$ $\square$
4. $28.21 \times 8.02 \approx$
$17.5 \times 8.4 \approx$
5. $71.92 \times 2.01 \approx$
6. On average, the U.S. produces 36.5 million tons of fruit each year. About how much fruit does it produce in 2.25 years? (Examples 3 and 4)
$\qquad$
$\qquad$
7. Lisha is making headbands using ribbon. She would like to make 12 headbands. Each one requires 15.5 inches of ribbon. She estimates that she will need to buy 160 inches of ribbon. Is her estimate reasonable? Explain your reasoning. (Example 5)

19 Financial Literacy Hannah's hourly wage at the ice cream shop is $\$ 5.85$. The table shows the number of hours she worked. She estimates her earnings to be $\$ 120$. Without calculating her actual earnings, determine if her estimate is more or less than her actual earnings. Explain your reasoning.

| Day | Hours <br> Worked |
| :--- | :--- |
| Monday | 3.5 |
| Tuesday | 4.25 |
| Wednesday | 3.75 |
| Thursday | 2.5 |
| Friday | 4.75 |

10. Sill A car releases 19.6 pounds of carbon dioxide for every 1 gallon of gasoline burned. Estimate the number of pounds of carbon dioxide released if 14.5 gallons are burned.
11. CCGPS Model with Mathematics Refer to the graphic novel frame below for Exercises a-b.

a. How much more does Raj need until he has enough to buy the video game system?
b. Raj estimates that if he works for 20 hours, he will have enough to buy the video game system. Is he correct? Explain.

## H.O.T. Problems Higher Order Thinking

12. CCGPS Reason Abstractly Name three decimals with a product that is about 40.
13. CCGFS Persevere with Problems A scooter can travel between 22 and 28 miles on each gallon of gasoline. If one gallon of gasoline costs between $\$ 3.75$ and $\$ 3.95$ per gallon, about how much will it cost to travel 75 miles?
14. CCGFSS Justify Conclusions Suppose your friend multiplied 1.2 and
 2.6 and got 31.2 as the product. Is your friend's answer reasonable? Justify your response.

## Georgia Test Practice

15. Green peppers are on sale for $\$ 2.89$ per pound. Mrs. Moseley bought 1.75 pounds of peppers. About how much did she pay for the peppers?
(A) less than $\$ 4$
(C) between $\$ 6$ and $\$ 7$
(B) between $\$ 5$ and $\$ 6$
(D) more than
\$7
$\qquad$

## Extra Practice

## Estimate each product.

16. $26.3 \rightarrow 26$
$\times 9.7 \rightarrow \times 10$
$26 \times 10=260$
Homework
Help
17. 33.6
$\times 82.1$
18. 99.1
$\times 11.2$
19. Sinn A single year on Saturn is equal to 29.4 years on Earth. About how many Earth-years are equal to 3.2 years on Saturn?
20. Miguel received a $\$ 50$ gift card to a bookstore. He would like to buy 3 books that cost $\$ 15.75$ each including tax. He estimates that he cannot buy all three books because each book costs about $\$ 20$, and all three books would cost $\$ 60$. Is his estimate reasonable? Explain your reasoning.
$\qquad$
$\qquad$

Use estimation to determine whether each answer is reasonable. If the answer is reasonable, write yes. If not, write no and provide a reasonable estimate.
21. $22.8 \times 4.7=107.16$ $\qquad$
23. $7.8 \times 1.1 \times 4.2=50$
25. CCGFS Use Math Tools The table shows some
22. $2.1 \times 4.9 \times 7.2=105.84$
24. $43.8 \times 2.8 \times 3.1=371.8$
nutritional facts about orange juice. Estimate each value for 1 quart of orange juice.
(Hint: 4 cups is equal to 1 quart.)


## Georgia Test Practice

26. Mario and Andrew's hourly charge for mowing lawns is shown.

| Mario | Andrew |
| :---: | :---: |
| $\$ 8.25 / \mathrm{h}$ | $\$ 5.85 / \mathrm{h}$ |

Suppose Mario and Andrew each worked 20 hours. About how much more money did Mario earn?
(A) $\$ 30$
(C) $\$ 60$
(B) $\$ 40$
(D) $\$ 70$
27. Short Response Javier bought 4 pencil toppers at the school store for $\$ 3.69$ each. He estimated how much he needed to pay and gave the cashier \$16. Is Javier's estimation reasonable? Explain your reasoning.
28. The Student Book Club is ordering 12 copies of a book. The books cost $\$ 8.99$ each. About how much will the order cost?
(F) $\$ 90$
(H) $\$ 120$
(G) $\$ 108$
(1) $\$ 135$
29. Medina's school lunch menu is shown.

| Friday |  |  |  |
| :--- | ---: | :--- | ---: |
| Pizza | $\$ 1.75$ | Fruit Punch | $\$ 0.75$ |
| Fish and | Fries | $\$ 2.25$ | Milk |
| Salad | $\$ 1.15$ | Pudding | $\$ 0.80$ |

Which of the following is a reasonable estimate for the cost of two slices of pizza, a salad, and fruit punch?
(A) $\$ 4$
(C) $\$ 8$
(B) $\$ 6$
(D) $\$ 10$

## Common Core Review

Multiply. mcc5.NBT. 5
30. 65

| $\times 18$ |
| :--- |

31. 15
$\begin{array}{r} \\ \times 23 \\ \hline\end{array}$
32. 198
$\begin{array}{r}15 \\ \times \quad \\ \hline\end{array}$
33. Marissa spent $\$ 15.63$ at the bookstore. She paid with a $\$ 20$ bill. How much change will she receive? мсс5.пвт. 7 $\qquad$ $\underline{ }$
34. Cristian is placing photos onto scrapbook paper for his photo album. The scrapbook paper is 12 inches long and 12 inches wide. What is the area of the paper?
(Hint: area $=$ length $\times$ width ) mсс4.MD. 3


## marcioly Dectmall by Whole Numbers

## What You'll Learn

Scan the lesson. List two headings you would use to make an outline of the lesson.

## Real-World Link

Plants Bamboo is one of the fastest growing plants. It can grow about 4.9 feet in height per day. It is a favorite food of panda bears. You can use repeated addition to find the total height a bamboo plant can grow over a number of days. Complete the table below. The first one is done for you.
1.
2.
3.

| Number <br> of Days | Repeated Addition |  |  |  |  | Multiplication |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 4.9 | +4.9 | $=9.8$ |  |  | $2 \times 4.9=9.8$ |
| 3 | + | + | $=$ |  |  | $\times 4.9=$ |
| 4 | + | + | + | $=$ |  | $\times 4.9=$ |
| 5 | + | + | + | + | $=$ | $\times 4.9=$ |

4. Use the pattern in the table to predict $6 \times 4.9$.

Check by using repeated addition.
5. CCCRS Make a Conjecture Look back at Exercises 1-4. Compare the number of decimal places in each factor to the number of decimal places in the product. How do you determine the placement of the decimal oint in a product?
$\qquad$
$\qquad$

$\qquad$

## Multiply Decimals

Using repeated addition can help you place the decimal point. The whole number represents the number of times the decimal is used as an addend. So, place the decimal point in the product the same number of places from the right as the decimal factor.

## Examples

1. Find $\mathbf{4} \times \mathbf{0 . 8 3}$.

Estimate $4 \times 1=4$
$0.83 \longleftarrow$ two decimal places
0.83
$\times \quad 4$
3.32 Place the decimal point two places from the right.

Check for Reasonableness $3.32 \approx 4 \checkmark$
2. Find $3 \times 14.2$.

Estimate $3 \times 14=42$
$14.2 \longleftarrow$ one decimal place


4 groups of 0.83
14.
$\times \quad$
42.6 Place the decimal point one place from the right.

Check for Reasonableness $42.6 \approx 42 \checkmark$

## 3. Find $4 \times 0.95$.

Estimate $4 \times \square=\square$ Use the bar diagram to find the product.


Place the decimal point $\square$ places from the right.

Check for Reasonableness


## Got It? Do these problems to find out.

a. $5 \times 0.25$
b. $8 \times 4.47$
c. $9 \times 2.63$

## Annex Zeros in the Product

If there are not enough decimal places in the product, you need to annex zeros to the left. To annex a zero means to place a zero at the beginning or end of a decimal.

## Examples


4. Find $2 \times 0.018$.

5. Find $4 \times 0.012$.

| 0 . 0 | 1 | 2 | 0.012 has | decimal places. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| + 4 |  |  |  | to make | decimal places. |
|  |  |  | Annex a |  |  |
| Check by Adding | 0 | 0 | 1 |  |  |
|  | 0 | 0 | 1 |  |  |
|  | 0 | 0 | 1 |  |  |
|  | + 0 | 0 | 1 |  |  |
|  |  |  |  | $\checkmark$ |  |

Got It? Do these problems to find out.
d. $3 \times 0.02$
e. $0.12 \times 8$
f. $11 \times 0.045$
e. $\qquad$
f. $\qquad$

## Example


6. A batch of trail mix calls for 1.2 pounds of dry cereal. Nigela is making 5 batches of trail mix. She already has 2.2 pounds of cereal. How many more pounds of dry cereal does she need?

Step 1 Multiply.
$1.2 \longleftarrow$ one decimal place
$\frac{\times 5}{6.0} \longleftarrow$ one decimal place

Step 2 Subtract.
6.0

$$
\frac{-2.2}{3.8}
$$

So, Nigela will need 3.8 more pounds of dry cereal.

## Guided Prectice

Multiply. (Examples 1-5)

1. $2.7 \times 6=$ $\qquad$
2. $0.52 \times 3=$ $\qquad$ 3. $5 \times 0.09=$ $\qquad$
3. $4 \times 0.027=$ $\qquad$
4. $0.071 \times 8=$ $\qquad$ 6. $0.065 \times 18=$ $\qquad$
5. A bee hummingbird has a mass of 1.8 grams. How many grams are 6 hummingbirds and a 4-gram nest?
(Example 6)
6. Justin buys 12 pencils for $\$ 0.56$ each. He pays with a $\$ 10$ bill. How much change will he receive? (Example 6)
7. © Building on the Essential Question How can estimating products help you to place the decimal correctly?

## Rate Yourself!

Are you ready to move on?
Shade the section that applies.


For more help, go online to access a Personal Tutor.
$\qquad$

## Independent Practice

Multiply. (Examples 1-5)

## 1. $1.2 \times 7=$


4. $0.8 \times 9=$ $\qquad$

1 The table shows the number of gallons of gasoline the Beckleys purchased on their road trip. What was the total cost for gas for the trip? (Example 6)
$\qquad$
$\qquad$

| Fuel |  |
| :---: | :---: |
| Number of Gallons | Cost per Gallon (\$) |
| 12 | 4.89 |
| 17 | 4.72 |
| 15 | 5.09 |

8. Sharon buys 14 folders for $\$ 0.75$ each. How much change will she receive if she pays with $\$ 15$ ? (Example 6)
$\qquad$
$\qquad$
9 Silam The hottest temperature recorded in the world, in degrees Fahrenheit, can be found by multiplying 13.46 by 10 . Find this temperature. Justify your procedure.
9. CCGFS Justify Conclusions Asher recently bought the poster shown at the right. What is its area? Explain your reasoning to a classmate. (Hint: Use area $=$ length $\times$ width. $)$
$\qquad$
$\qquad$
$\qquad$

10. CCGRS Use Math Tools The thickness of each type of coin is shown in the table. How much thicker is a stack of a dollar's worth of nickels than a dollar's worth of quarters? Explain your answer.

## H.O.T. Problems Higher Order Thinking

12. CCGFS Model with Mathematics Write a real-world problem involving multiplication by a decimal factor. Then solve the problem.
13. CCGFS Persevere with Problems Discuss two different ways to find the value of the expression $5.4 \times 1.17 \times 100$ that do not require you to first multiply $5.4 \times 1.17$.
$\qquad$
$\qquad$
$\qquad$ $\longrightarrow$
14. CCGPS Reason Inductively Use the product of $123 \times 47$ to find the product of $123 \times 0.47$. Explain the difference in the two products.
15. CCCFPS Construct an Argument Your friend thinks that $1.5 \times 8=1.20$ because you do not count the zero when placing the decimal point. Is your friend correct? Justify your reasoning.

## Georgia Test Practice

16. Anita bought 3 bags of sugar. Each bag weighed 36.8 ounces. How many ounces of sugar did she buy?
(A) 11.04
(C) 110.4
(B) 73.6
(D) 120.8
$\qquad$

## Extra Practice

Multiply.

18. $0.9 \times 4=$ $\qquad$
21. $7 \times 0.012=$
20. $3 \times 0.5=$ $\qquad$
$\qquad$
19. $2.4 \times 8=$ $\qquad$
22. $0.0198 \times 75=$ $\qquad$
23. The mass of a certain monarch butterfly is 0.56 gram. What is the mass of 4 monarch butterflies?
24. The height of Mount Everest, in meters, can be found by multiplying 8.85 by 1,000. Find the height of Mount Everest. Explain your answer.
26. Sofia bought 12 pens for $\$ 0.59$ each. She paid with a $\$ 10$ bill. How much change will she receive?
25. A sheet of printer paper is 8.5 inches by 11 inches. What is the area of the paper? (Hint: area $=$ length $\times$ width $)$
27. CCGFS Be Precise One kilometer is about 0.62 mile. It is 12 kilometers from Noah's house to the ice skating rink. About how many miles is it from Noah's house to the ice skating rink?

## Georgia Test Practice

28. Short Response The school store is selling the following items.

| Item | Price |
| :--- | :---: |
| Pennant | $\$ 2.49$ |
| Bumper Sticker | $\$ 1.79$ |
| Magnet | $\$ 0.89$ |

If Miguel buys two pennants, two bumper stickers, and four magnets, how much will he spend for all the items?
29. Short Response Find the area of the rug shown.

30. The table shows the admission prices to an amusement park.

| Admission Prices | One-Day Pass | Two-Day Pass |
| :--- | :---: | :---: |
| Adult | $\$ 39.59$ | $\$ 43.99$ |
| Child (ages 3-9) | $\$ 30.59$ | $\$ 33.99$ |

What is the total price of one-day passes for two adults and three children?
(A) $\$ 140.36$
(B) $\$ 170.95$
(C) $\$ 179.95$
(D) $\$ 189.95$

## Common Core Review

Round each decimal to the nearest whole number. MCC5.Nвт. 4
31. $5.7 \approx$
32. $0.05 \approx$
33. $13.49 \approx$
34. Use number patterns and powers of ten to complete the table. мсс5.NBT. 2

| Factor | $\times$ | Factor | $=$ | Product |
| :---: | :---: | :---: | :---: | :---: |
| 2.9 |  | 10 |  |  |
| 3.44 | $\times$ |  | $=$ | 344 |
|  | $\times$ | 100 | $=$ | 870 |
| 10.25 | $\times$ |  | = | 102.5 |
| 156.23 | $\times$ | 10 | $=$ |  |

35. Several students from Southbend Middle School are visiting the Smithsonian American Art Museum. Mrs. Mabika divided the students into 5 equal groups. There are 3 boys and 4 girls in each group. Fill in the missing numbers to find the total number of students. mcc5.0А. 2
$\square \times(\square+4)=\square$ students

## Marredily Decimala by Dectmals

## What You'll Learn

Scan the lesson. List two real-world scenarios in which you would multiply a decimal by a decimal.
$\qquad$
-

## RealWorldLink

Planets The table shows the weight of a 1-pound object on each planet.

| Planet | Weight (Pounds) |
| :--- | :---: |
| Mercury | 0.3 |
| Venus | 0.9 |
| Earth | 1 |
| Mars | 0.3 |
| Jupiter | 2.3 |
| Saturn | 1 |
| Uranus | 0.8 |
| Neptune | 1.1 |



1. A 0.5 -pound object weighs one half as much as a 1-pound object. If a cheeseburger weighs a half pound on Earth, what will it weigh on Jupiter?
2. What would a barbell that weighs 5 pounds on Earth weigh on Jupiter?
3. Use the results from Exercises 1 and 2 to find $0.05 \times 2.3$.

Explain your answer.


## Multiply Decimals

When multiplying a decimal by a decimal, multiply as with whole numbers. To place the decimal point, find the sum of the number of decimal places in each factor. The product has the same number of decimal places.

## Examples

1. Find $3.6 \times 0.05$.

Estimate $3.6 \times 0.05 \rightarrow 4 \times 0$ or 0

| 3.6 | $\leftarrow$ one decimal place |
| ---: | :---: |
| $\times 0.05$ | $\leftarrow$ two decimal places |
| 0.180 | $\longleftarrow$ three decimal places |

The product is 0.180 or 0.18 . $\begin{aligned} & \text { you can drop the zero at the right. }\end{aligned}$
2. Find $0.112 \times 7.2$.

Estimate $0.112 \times 7.2 \approx \square \times \square$ or $\square$
0.112 has

7.2 has $\square$ decimal place.
So the product has $\square+\square$, or $\square$ decimal places.


The product is $\qquad$ .

Check for reasonableness $\approx \quad \checkmark$

Got It? Do these problems to find out.
a. $5.7 \times 2.8$
b. $4.12 \times 0.05$
c. $0.014 \times 3.7$

## AnnexaZero

If there are not enough decimal places in the product, you need to annex zeros to the left.

## Examples

3. Find $1.4 \times \mathbf{0 . 0 6 7}$.

| 0.067 | $\leftarrow$ three decimal places |
| :--- | :--- |
| $\times \quad 1.4$ | $\leftarrow$ one decimal place |
| 268 |  |
| $+\quad 67$ |  |
| 0.0938 | $\leftarrow$ Annex a zero to make four decimal places. |

## 4. Find $0.45 \times 0.053$.

The product will have
decimal places. Annex zeros, if needed.


Check Multiply related whole numbers.


Move the decimal to the left 5 places. What is the number? Is the answer the same? $\qquad$ d. $\qquad$
e. $\qquad$
d. $0.04 \times 0.32$
e. $0.26 \times 0.205$
f. $1.33 \times 0.06$

## Got It? Do these problems to find out.

f.

## Example

5. A certain car can travel 28.45 miles with one gallon of gasoline. The gasoline tank can hold 11.5 gallons. How many miles can this car travel on a full tank of gas? Justify your answer.

Estimate $28.45 \times 11.5 \rightarrow 30 \times 12$ or 360

| 28.45 | $\leftarrow$ two decimal places |
| :---: | :---: |
| $\frac{\leftarrow 11.5}{14225}$ | $\leftarrow$ one decimal place |
| 2845 |  |
| +2845 <br> 327.175 | $\leftarrow$ The product has three decimal places. |

The car could travel 327.175 miles. Since $327.175 \approx 360$, the answer is reasonable.

## Guided Practice

Multiply. (Examples 1-4)

1. $0.6 \times 0.5=$
2. $27.43 \times 1.089=$
3. $0.98 \times 7.3=$
4. $2.7 \times 1.35=$
5. $0.03 \times 0.09=$
6. $0.04 \times 2.12=$
7. A mile is equal to approximately 1.609 kilometers. How many kilometers is 2.5 miles? Justify your answer. (Example 5)

## Rate Yourself!

Are you ready to move on? Shade the section that applies.


For more help, go online to access a Personal Tutor.

## Independent Practice

Multiply. (Examples 1-4)

1. $0.7 \times 0.4=$

$\qquad$ 2. $0.4 \times 3.7=$ $\qquad$ $130.52 \times 2.1=$
2. $6.2 \times 0.03=$ $\qquad$
3. $14.7 \times 11.361=$ $\qquad$ 6. $0.28 \times 0.08=$ $\qquad$

17 sidan A giraffe can run up to 46.93 feet per second. How far could a giraffe run in 1.8 seconds? Justify your answer. (Example 5)
$\qquad$
$\qquad$
8. A nutrition label indicates that one serving of apple crisp oatmeal has 2.5 grams of fat. How many grams of fat are there in 3.75 servings? Justify your answer. (Example 5)
$\qquad$
$\qquad$
19 Financial Literacy Pears cost $\$ 0.92$ per pound and apples cost $\$ 1.10$ per pound. Mr. Bonilla bought 3.75 pounds of pears and 2.1 pounds of apples. How much did he pay for the pears and apples? Explain your answer.
$\qquad$
$\qquad$

## Multiply.

10. $25.04 \times 3.005=$ $\qquad$ 11. $1.03 \times 1.005=$ $\qquad$ 12. $5.12 \times 4.001=$ $\qquad$
11. cCGPS Use Math Tools Complete the graphic organizer to show the relationship between decimal factors and their products.

| $\times$ | 2 | $\mathbf{0 . 2}$ | $\mathbf{0 . 0 2}$ | $\mathbf{0 . 0 0 2}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{3}$ | $\mathbf{6}$ | 0.6 | 0.06 |  |
| $\mathbf{0 . 3}$ |  | 0.06 | 0.006 | 0.0006 |
| $\mathbf{0 . 0 3}$ | 0.06 | 0.006 |  |  |
| $\mathbf{0 . 0 0 3}$ |  | 0.0006 |  |  |

How do you determine the number of zeros to annex in the product of 0.002 and $0.003 ?$

## H.O.T. Problems Higher Order Thinking

14. CCGPS Reason Abstractly Write a multiplication problem in which the product is between 0.05 and 0.75 .
15. CCGPS Justify Conclusions Place the decimal point in the answer to make it correct. Explain your reasoning. $3.9853 \times 8.032856=32013341 \ldots$
16. CCGPS Construct an Argument Determine whether the following statement is always, sometimes, or never true. Give examples to justify your answer.

The product of two decimals less than 1 is less than either of the factors.
17. CCGFS Reason Inductively Is the product of $0.4 \times 1.8$ greater than or less than 0.4? Explain your reasoning.
18. CCCYS Persevere with Problems Evaluate the expression $0.3(3-0.5)$.

## Georgia Test Practice

19. What is the area of the rectangle?
(A) $14.04 \mathrm{~cm}^{2}$
(C) $8.992 \mathrm{~cm}^{2}$
(B) $10.248 \mathrm{~cm}^{2}$
(D) $7.868 \mathrm{~cm}^{2}$


## ExtraPractice

## Multiply.

20. $1.5 \times 2.7=4.05$
1.5
$\left.\begin{array}{c}\text { Homework } \\ \text { Help }\end{array}\right) \frac{2.7}{105}$
105

$$
\begin{aligned}
& +30 \\
& \hline 4.05
\end{aligned}
$$

23. $5.04 \times 3.2=$ $\qquad$
24. $3.1 \times 0.8=$ $\qquad$ 22. $2.4 \times 3.48=$
25. $0.451 \times 0.05=$ $\qquad$
26. $27.4 \times 33.68=$ $\qquad$
27. Katelyn has a vegetable garden that measures 16.75 feet in length and 5.8 feet in width. Find the area of the garden. Justify your answer.
28. CCGPS Use Math Tools Find examples of decimals in a newspaper or magazine, on television, or on the Internet. Write a realworld problem in which multiplies decimals.
$\qquad$ $\xrightarrow{ }$
29. CCGTS Be Precise Find the area of the figure at the right. Justify your procedure.
$\qquad$ $\xrightarrow{ }$

30. Junnie walked for 2.5 hours at a speed of 3.2 miles per hour. Maurice walked for 1.8 hours at a speed of 4.1 miles per hour. (Hint: Distance equals speed times time.)
a. Who walked farther? $\qquad$
b. How much farther did that person walk? $\qquad$


## Georgia Test Practice

30. The grocery store is selling bananas for $\$ 0.35$ per pound. How much will Zack pay for 3.6 pounds of bananas?

(A) $\$ 1.26$
(C) $\$ 3.95$
(B) $\$ 1.40$
(D) $\$ 12.60$
31. A turtle can walk up to 0.69 mile per hour. At this rate, how far could a turtle walk in 1.75 hours?
(F) 0.1208 miles
(-1) 2.44 miles
(G) 1.2075 miles
(1) 12.075 miles
32. Short Response $A$ soccer ball and 12 golf balls have a total mass of 1 kilogram. The mass of each golf ball is about 0.046 kilogram. What is the mass of the soccer ball?
33. Short Response Renaldo can rollerblade 9.7 miles per hour. At this rate, how far will he rollerblade in 0.75 hour?

## (CCGPS Common Core Review

Divide. мсс5.лвт. 6
34. $60 \div 12=$ $\qquad$ 35. $96 \div 8=$ $\qquad$ 36. $750 \div 15=$ $\qquad$
37. Logan has 20 action figures. He is shipping them to a friend. He can fit 3 action figures in a box. How many boxes will he need? mсс5.nвт. 6
$\qquad$
38. Three friends are dividing the cost of a kite equally. The kite costs $\$ 15.75$. How much will each person pay? mcc5.nвт. 7


# Inquiry Lab <br> Multiply by Powers of Ten 

HOW can number patterns be used to multiply by powers of 10 ?

Content Standards MCC6.NS. 3
Mathematical Practices
1, 3, 5

Planets Each planet in our solar system orbits around the Sun at a different distance from the Sun. Mercury orbits at an average distance of 28.6 million miles. One million is $1,000,000$. What is $28.6 \times 1,000,000$ ?

What do you know?
What do you need to know?


| Decimal |  | Power of 10 |  | Product |
| :---: | ---: | ---: | ---: | ---: | ---: |
| 28.6 | $\times$ | 0.1 | $=$ | 2.86 |
| 28.6 | $\times$ | 1 | $=$ | 28.6 |
| 28.6 | $\times$ | 10 | $=$ | 286 |
| 28.6 | $\times$ | 1,000 |  | 28,600 |

Move the decimal point the $\qquad$ number of places as the number of zeros in the power of 10.

Move the decimal point to the $\qquad$ when multiplying by a power of 10 that is less than 1.

Move the decimal point to the $\qquad$ when multiplying by a power of 10 that is greater than 1.

Step 2 Determine how many zeros are in 1,000,000 and move the decimal point in 28.6 the appropriate number of places.

There are $\square$ zeros in 1,000,000.

$$
\begin{aligned}
28.6 \text { million } & =28.6 \times 1,000,000 \\
& =28.600000 \\
& =28,600,000
\end{aligned}
$$

## Analyze

Use Math Tools Work with a partner to complete the tables.

| Decimal | Power of 10 |  |  | Product |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  | 12.4 | $\times$ | 0.1 | $=$ | 1.24 |
| 1. | 12.4 | $\times$ | 0.01 | $=$ |  |
| 2. | 12.4 | $\times$ | 0.001 | $=$ |  |
| 3. | 12.4 | $\times$ | 0.0001 | $=$ |  |

4. 

| Decimal | Power of 10 |  |  | Product |
| :--- | :--- | :--- | :--- | :--- |
| 1.24 | $\times$ | 1 | $=$ | 1.24 |
| 1.24 | $\times$ | 10 | $=$ |  |
| 1.24 | $\times$ | 100 | $=$ |  |
| 1.24 | $\times$ | 1,000 | $=$ |  |
| 1.24 | $\times 10,000$ | $=$ |  |  |
| 1.24 | $\times 100,000$ | $=$ |  |  |
| 1.24 | $\times 1,000,000$ | $=$ |  |  |
| 1.24 | $\times 10,000,000$ |  |  |  |

11. CCCAS Reason Inductively How can you find the product of a number and power of 10 without using paper and pencil or a calculator? $\qquad$
12. CCGPS Reason Inductively The product of 13.6 and a power of 10 is 13,600 . What is the power of 10 ? Explain.

## Reflecs

13. cccis Use Math Tools Suppose you plan to purchase 10 items that each cost $\$ 4.95$. Explain how to use mental math to find the cost of the 10 items.
14. Inquiry HOW can number patterns be used to multiply by powers of 10 ?

## Problem-Solving Investigation Look for a Pactern

## Case \#1 Dance Party

The Student Government is organizing a spring dance. They plan to decorate with helium-filled balloons. The cost of the balloons is shown in the table.
What is the cost of 6 bags of balloons?

Content Standards
MCC6.NS. 3
Mathematical Practices 1, 3, 4, 8

| Number of Bags | Total Cost (\$) |
| :---: | :---: |
| 1 | 4.75 |
| 2 | 9.50 |
| 3 | 14.25 |
| 4 | 19.00 |

## Understand what are the facts?

The table shows the cost of the balloons. Six bags of balloons are needed.


Plan What is your strategy to solve this problem?
Look for a pattern in the table. Each bag costs \$4.75.
Solve How can you apply the strategy?
Complete the table to find the cost of 6 bags of balloons.

| Number of Bags | Total Cost (\$) |
| :---: | :---: |
| 1 | 4.75 |
| 2 | 9.50 |
| 3 | 14.25 |
| 4 | 19.00 |
| 5 |  |
| 6 |  |

So, six bags of balloons cost \$


## Check Does the answer make sense?



Use multiplication to check your answer. $\$ 4.75 \times 6=$ $\qquad$

## Analyze the Strategy

Reason Inductively How would the results change if the store offered a discount of $\$ 0.50$ for each bag of balloons?

## Case \#2 Virtual DJ

The Student Government is hiring a DJ for the spring dance. They expect the dance to last for 5 hours. The cost to hire DJ Trax is shown in the table.
How much will it cost to hire DJ Trax for the dance?

## 

## Understand

Read the problem. What are you being asked to find?
I need to

| Cost to Hire <br> DJ Trax |  |
| :---: | :---: |
| Number <br> of Hours | Total <br> Cost (\$) |
| 1 | 125.50 |
| 2 | 251.00 |
| 3 | 376.50 |

Underline key words and values in the problem. What information do you know?
The cost to hire DJ Trax is \$__ for 1 hour, $\$$ for
2 hours, and \$ for 3 hours.
Is there any information that you do not need to know?
I do not need to know
Plan
Choose a problem-solving strategy.
I will use the $\longrightarrow$ strategy.

## Solve

Use your problem-solving strategy to solve the problem.
Describe the pattern. Then complete the table.
The cost to hire DJ Trax
by \$
for each hour.

| Cost to Hire DJ Trax |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Number of Hours | 1 | 2 | 3 | 4 |
| Total Cost (\$) | 125.50 | 251.00 | 376.50 |  |

Collaborate Work with a small group to solve the following cases. Show your work on a separate piece of paper.

## Case \#3 Gaming

The table below shows the cost of a subscription to the Action Gamers Channel.

| Action Gamers Channel Prices |  |
| :---: | :---: |
| Number of Months | Total Cost (\$) |
| 1 | 7.95 |
| 2 | 15.90 |
| 3 | 23.85 |

What is the cost of a 6 -month subscription?


## Case \#4 Number Theory

The diagram to the right is known as Pascal's Triangle.
If the pattern continues, what will the numbers in the next row be from left to right?


## Case \#5 Number Sense

Describe the pattern below. Then find the next three numbers.

$$
3,6.5,11,16.5,23
$$

Circle a strategy below to solve the problem. - Make a model.

- Make a table.
- Solve a simpler problem.
- Guess, check, and revise.


## Case \#6 Games

Claudio is purchasing a new gaming system. One Web site sells the system for $\$ 240$ and the games for $\$ 45.99$ each.

What is the total cost if Claudio purchases the system and 3 games?

## Mid=Chapter Check

## Vocabulary Check

1. Define product. Give an example of two whole number factors with a product of 9 .

## Skills Check and Problem Solving

Find each sum or difference. (Lesson 1)
2. $42.7+52.12=$ $\qquad$
3. $4.7-3.28=$ $\qquad$ 4. $8.37-0.015=$ $\qquad$

Multiply. (Lessons 3 and 4)
5. $2.3 \times 5=$ $\qquad$
6. $3.4 \times 5.2=$ $\qquad$ 7. $1.2 \times 0.015=$
8. The table shows a list of walking trails in the United States. Latisha walked the KATY Trail 6 days last week. How many miles did she walk in a week. (Lesson 3)
9. CcGFS Be Precise The length of a pool table is 7.1 feet and the width is 3.6 feet. Find the area of the surface of the pool table by multiplying the length by the width. (Lesson 4)

| Location | Length of Trail (mi) |
| :--- | :---: |
| Florida Trail (FL) | 4.8 |
| Long Path (NJ) | 3.3 |
| Ohio \& Erie Canal <br> Trail (OH) | 4.3 |
| KATY Trail (MO) | 5.7 |
| Point Reyes National <br> Seashore (CA) | 5.0 |

10. Georgia Test Practice Ashton used 12.6 gallons of gasoline to drive his car on a weekend trip. He averaged 21.5 miles per gallon. About how many miles did he travel? (Lesson 2)
(A) 20 miles
(C) 350 miles
(B) 200 miles
(D) 400 miles

## Divide Murfi-Digit Mumbere

## What You'll Learn

Scan the lesson. Predict two things you will learn about dividing multi-digit numbers.

## Vocabulary Start-Up

When one number is divided by another, the result is called a quotient. The dividend is the number that is divided and the divisor is the number used to divide another number.

Label the division problem with the correct vocabulary term: quotient, dividend, and divisor.


## Real-World Link

Circulation When you are at rest it takes about 60 seconds for a single blood cell to travel around your body and back to your heart.

1. In 120 seconds, about how many times does a single blood cell travel around your body and back to your heart? Write the dividend, divisor, and quotient in the diagram below.
2. Camila's target heart rate should be about 200 beats per minute. Estimate the number of times Camila's heart will beat in one second if her heart is working at this rate. Explain.

## Essential Question

HOW can estimating be helpful?

## Common Core GPS

## Content Standards

MCC6.NS. 2
Mathematical Practices
1, 2, 3, 4, 5, 6


## Divide Three-Digit Dividends

In this lesson, you will divide multi-digit numbers. Use estimation to help you place the first digit in the quotient.

## Examples

1. Find $351 \div 9$.

Estimate $360 \div 9=40$. So, the first digit is in the tens place.
Write $351 \div 9$ as $9 \longdiv { 3 5 1 }$.
$\begin{array}{r}39 \\ 9 \\ \hline 351\end{array}$
Divide each place-value position from left to right.
$-27$
81
$-81$ Since $81-81=0$, there is no remainder.

So, $351 \div 9$ is 39 .
Check Compare 39 to the estimate. $39 \approx 40$
2. Find $3 1 \longdiv { 8 7 8 }$.

Estimate $900 \div 30=30$. So, the first digit is in the tens place.
$\begin{array}{ll}\begin{array}{l}\text { 31 } \\ \begin{array}{l}878 \\ \frac{-62}{258}\end{array} \\ \frac{-248}{10}\end{array} \quad \text { Divide each place-value position from left to right. } \\ & \\ & \text { Since } 258-248=10 \text { and } 10<31,10 \text { is the remainder. }\end{array}$
So, $3 1 \longdiv { 8 7 8 }$ is 28 R 10 .
Check 28 R10 $\approx 30 \boldsymbol{V}$

Got It? Do these problems to find out.
Find each quotient.
a. $768 \div 8$
b. $1 6 \longdiv { 3 1 8 }$

## Divide Four-Digit Dividends

The steps for dividing three-digit dividends and four-digit dividends are the same.

## Examples

## 3. Find $6,493 \div 75$.

Estimate $6,400 \div 80=80$

| 86 |
| ---: |
| $7 5 \longdiv { 6 , 4 9 3 }$ |
| -600 <br> 493 <br> -450 <br> 43 |

Check for Reasonableness 86 R43 $\approx 80 \checkmark$
The quotient of $6,493 \div 75$ is 86 R43.

## 4. The average person has 1,460 dreams a year. What is the average number of dreams a person has each night?

Find 1,460 $\div 365$.
Estimate $1,600 \div 400=4$
4
$3 6 5 \longdiv { 1 , 4 6 0 }$
$-1,460$
0
Check for Reasonableness $4=4 \quad \checkmark$
The average number of dreams a person has each night is 4 .

Got It? Do these problems to find out.
c. Find $5 6 \longdiv { 4 , 3 2 1 }$.
d. Find $9 1 \longdiv { 8 , 4 6 5 }$.
e. To promote its opening weekend, a water park gave the local middle school 1,050 free tickets. The middle school has 350 students. Each student will receive the same number of tickets. How many tickets will each student receive?

## Check Your Answer

You can check division with a remainder. Multiply the quotient by the divisor. Then add the remainder.

$$
\begin{array}{r}
86 \\
\times 7545 \\
\times \quad 75 \\
\hline 6,450 \\
\hline 6,493
\end{array}
$$

## Example

5. The total number of seats in a college stadium is 54,912 . There are 44 sections and each section has an equal number of seats. How many seats are in each section?

Divide 54,912 by 44 .

| $\frac{1,248}{44} \begin{array}{l}\frac{-44}{54,912} \\ \frac{-88}{211} \\ \frac{-176}{352} \\ \frac{-352}{0}\end{array}$ |
| :--- |

There are 1,248 seats in each section.

## Guided Practice

Find each quotient. (Examples 1-4)

1. $8 \longdiv { 7 3 6 }$
2. $1 1 \longdiv { 6 2 0 }$
3. $1 9 \longdiv { 7 , 8 1 4 }$
4. $3 7 \longdiv { 3 , 5 1 1 }$
5. Zach bought two new jet skis for $\$ 15,480$. He will make 36 equal payments. How much will each payment be?
(Example 5)

## Rate Yourself!

How well do you understand dividing multi-digit numbers? Circle the image that applies.


For more help, go online to access a Personal Tutor.
6. Building on the Essential Question How is estimation helpful when dividing multi-digit numbers?
$\qquad$
$\qquad$
$\qquad$

$\qquad$

## Independent Practice

Find each quotient. (Examples 1-3)

1. $174 \div 6=$

$\sqrt { 5 } 6 2 \longdiv { 8 , 0 9 0 }$
2. $453 \div 8=$
3. $645 \div 43=$
4. $3 4 \longdiv { 5 , 7 8 0 }$
5. $3 1 \longdiv { 2 , 4 8 0 }$ $\mid$

9 A tour bus travels 2,160 miles in 36 hours. What is the average distance the bus travels in one hour? (Example 4)
10. A charity sold 475 tickets to a dinner auction. If the charity raised $\$ 16,625$ in ticket sales, what was the cost of one ticket? (Example 5)
11. A city phone book has 86 pages filled with residents' names. There are a total of 15,050 names in the book. Each page has an equal number of names on it. How many names are on each page? (Example 5)
12. CCGFS Use Math Tools The table shows the number of servings for different size cakes at Mimi's Bakery. Suppose a high school graduation expected 2,889 guests. How many X-large sheet cakes should the school order? Explain how you solved.
 -
$\qquad$
$\qquad$
$\qquad$
13. CCGPS Be Precise How many 8-ounce cups can be filled from 9 gallons of juice? (Hint: There are 128 ounces in one gallon.)
14. CCGPS Be Precise Water stations will be placed every 600 meters of a fifteen kilometer race. How many water stations will be needed? (Hint: There are 1,000 meters in one kilometer.)

## H.O.T. Problems Higher Order Thinking

15. CCGPS Model with Mathematics Write and solve a real-word problem that involves a two-digit divisor and a four-digit dividend.
16. CCGPS Persevere with Problems If the divisor is 40 , what is the least three-digit dividend that would give a remainder of 4 ?
17. CCGFS Justify Conclusions Can the remainder in a division problem ever equal the divisor? Why or why not?
18. CCGFS Reason Abstractly Use the digits 2,4 , and 8 one time each in the following problem.

$$
\square, \square 00 \div \square=30
$$

## Georgia Test Practice

19. The table shows the mileage Karla drove on her trip. She drove for a total of 24 hours. What is the average speed she drove?

| (A) 55 mph | Karla's Trip |  |
| :--- | :---: | :---: |
| (B) 60 mph | Day | Miles |
| (C) 65 mph | 1 | 486 |
| (D) 70 mph | 2 | 316 |
|  | 3 | 638 |

## ExtraPractice

Find each quotient.

24. $4 4 \longdiv { 2 , 8 7 6 }$
21. $345 \div 6=$
22. $792 \div 33=$
26. $3 3 \longdiv { 9 , 5 3 7 }$
23. $811 \div 79=$
27. $1 9 \longdiv { 4 , 2 5 7 }$
28. A city library has 9,440 nonfiction books. The librarian wants to divide the books evenly among 80 shelves. How many books will be on each shelf?
$\qquad$
30. ccGrs Use Math Tools The table shows the average weight of animals. How many more tons does a blue whale weigh than an African elephant? Explain how you solved. (Hint: There are 2,000 pounds in one ton.)
 pound in one ton.)

## Georgia Test Practice

31. The dance team recently purchased 25 pairs of new boots for $\$ 1,350$. What was the price of each pair of boots?
(A) $\$ 50$
(C) $\$ 55$
(B) $\$ 54$
(D) $\$ 60$
32. Short Response A toy factory assembles 19,824 toy castles over a 12-hour period of time. The same number of castles is assembled every hour. How many toy castles were assembled each hour?
33. The school auditorium holds 1,711 people. There are 59 seats in each row. How many rows of seats are in the auditorium?
(F) 23 rows
(H) 29 rows
(G) 25 rows
(1) 39 rows
34. Short Response The Carson Corporation distributed 58,992 sales fliers equally to 24 different cities. How many sales fliers were sent to each city?

## (CGAPS) Common Core Review

Divide mentally. mcc4.nBt. 6
35. $300 \div 5=$ $\qquad$ 36. $4,800 \div 8=$ $\qquad$
38. The maple tree in Logan's backyard is 58.6 feet tall. Plot 58.6 on the number line below. Then round 58.6 to the nearest whole number. mcc4.NF. 7
$\qquad$

39. There are 75 students attending a field trip. Each van will seat 8 students. How many vans will be needed? mсс4.nвт. 6
40. Mr. Maxwell is shipping 80 video games. Each box will hold 12 games. How many boxes will be needed? mсс4.nвт. 6

## Estimate Quotients

## What You'll Learn

Scan the lesson. List two headings you would use to make an outline of the lesson.

## Vocabulary Start-Up

To determine what a compatible number is, first you must determine what compatible means. Fill in the table below.

## Essential Question

HOW can estimating be helpful?

## Vocabulary

compatible numbers

## Content Standards

MCC6.NS. 2
Mathematical Practices
1, 3, 4, 5

| Definition: |  |  |
| :--- | :--- | ---: |
|  |  |  |
|  | Example: |  |
| What would make <br> numbers compatible? |  |  |
|  |  |  |



## Real-World Link

Remote Control Latasha and her two sisters want to buy their little brother a remote control helicopter. The helicopter costs $\$ 28.90$. They decided to split the cost equally.

1. What number that is a multiple of 3 is close to $\$ 28.90$ ? Explain.
2. Use your answer from Exercise 1 to determine about how much each person will pay. Explain.

## Estimate by Rounding Dividends

To estimate quotients of decimals, use rounding and compatible numbers. Compatible numbers are numbers that are easy to divide mentally.

## Examples

1. Estimate $11.75 \div 3$.

Round the dividend, 11.75, to a whole number.
The divisor is 3 . So, round 11.75 to a whole number that is a multiple of 3 .
$3 \longdiv { 1 1 . 7 5 } \rightarrow 3 \longdiv { \frac { 4 } { 1 2 } } \quad$ Using multiples of 3 , 12 is closest to 11.75
So, $11.75 \div 3$ is about 4 .
2. The Jenkins family bought five tickets to a charity auction. The receipt shows the total cost of the tickets. Estimate the cost of each ticket. Justify your answer.

$5 \longdiv { 6 1 . 2 5 } \rightarrow 5 \longdiv { 6 0 }$
Round 61.25 to 60 .
Each ticket costs about \$12.
Since $5 \times 12=60$ and $60 \approx 61.25$, the answer is reasonable.
Got It? Do these problems to find out.

## Estimate each quotient.

a. $49.3 \div 7$
b. $2 5 \longdiv { 9 8 . 1 }$
c. Suppose the Jenkins family decided to purchase 6 tickets for a total price of $\$ 64.50$ using a discount. Estimate the cost of each ticket. Justify your answer.

## Estimate by Rounding Divisors

You can also estimate quotients of decimals by rounding the divisors. Choose compatible numbers that are easy to divide mentally.

## Examples



## 3. Estimate $32 \div 3.9$.

Round the divisor, 3.9, to a whole number.
The dividend is 32 . So, round 3.9 to a whole number that is a factor of 32.
$3 . 9 \longdiv { 3 2 } \rightarrow 4 \longdiv { 8 2 } \quad$ Round 3.9 to 4 since 32 and 4 are compatible numbers.
So, $32 \div 3.9$ is about 8 .
Check by Multiplying $3.9 \times 8=31.2$

$$
31.2 \approx 32 \checkmark
$$

## 4. Estimate $56 \div 6.8$.

Round the divisor, $\square$ to a whole number.

The dividend is $\qquad$
So, round 6.8 to a whole number that is a of 56 .

Round 6.8 to $\qquad$ .

$6 . 8 \longdiv { 5 6 } \rightarrow \square \longdiv { 5 6 }$

So, $56 \div 6.8$ is about $\square$
Check by Multiplying $6.8 \times \square=\square$
$\square$
Round 6.8 to
. , ole number that is a .
$\square$都

## Got It? Do these problems to find out.

## Estimate each quotient.

d. $54 \div 9.16$
e. $1 0 . 7 5 \longdiv { 9 9 }$


How does the division fact $63 \div 9=7$ help you to estimate the quotient of $63 \div 8.4 ?$ Answer below.

## Example


5. Sill A Pacific Leatherback turtle can have a mass of up to 704.4 kilograms. An Olive Ridley turtle can have a mass of up to 49.9 kilograms. About how many times heavier is the Pacific Leatherback turtle? Explain why your answer is reasonable.
$4 9 . 9 \longdiv { 7 0 4 . 4 } \rightarrow 5 0 \longdiv { 1 4 } \quad$ Round 49.9 to 50 and 704.4 to 700 .
The Pacific Leatherback is about 14 times heavier than the Olive Ridley turtle.

Check for Reasonableness Since $50 \times 14=700$, and $700 \approx 704.4$, your answer is reasonable. $\checkmark$

Got It? Do this problem to find out.
f. There are approximately 250.9 million cars in the United States. Spain has approximately 25.1 million cars. About how many times more cars does the U.S. have than Spain? Explain why your answer is reasonable.

## Guided Practice

Estimate each quotient. (Examples 1, 3, and 4)

1. $25 \div 4.7 \approx$ $\qquad$ 2. $40.79 \div 7 \approx$ $\qquad$ 3. $3 8 . 1 \longdiv { 9 8 4 . 7 6 } \approx$ $\qquad$
2. STIM The average yearly precipitation for Gulfport, Mississippi, is 65.3 inches. About how much precipitation does the area receive each month? Explain why your answer is reasonable. (Example 2)
3. Mauricio bought 6.75 yards of fabric for a total of $\$ 47.50$. About how much was the cost per yard? Explain why your answer is reasonable. (Example 5)
4. Building on the Essential Question When is it helpful to estimate quotients? $\qquad$

## Rate Yourself!

How confident are you about estimating quotients? Shade the ring on the target.


For more help, go online to access a Personal Tutor.


## Independent Practice

Estimate each quotient.
(Examples 1, 3, and 4)

1. $32.4 \div 3 \approx$ $\qquad$ 2. $76.2 \div 18.4 \approx$ $\qquad$ 3. $1 1 . 4 \longdiv { 3 5 . 7 } \approx$
2. Financial Literacy Emily spent a total of $\$ 38.04$ on four CDs. If each CD cost the same amount, what is a reasonable amount for the cost of each CD? Explain why your answer is reasonable. (Example 2)

15 A recipe for a smoothie calls for 0.75 pound of strawberries. If Kerry has 3.15 pounds of strawberries, how many batches of the recipe can she make? (Example 5)
6. Financial Literacy For each handmade greeting card Jacqui sells, she makes a profit of $\$ 0.35$. In one week, she made a profit of $\$ 42$. She sells the cards for $\$ 0.75$ each.
a. About how many greeting cards did Jacqui sell that week?

b. About how much did she earn before paying expenses?

17 ccirs Justify Conclusions The average cow produces about 53 pounds of milk per day. If one gallon of milk weighs about 8.5 pounds, estimate the number of gallons of milk a cow produces each day. Explain why your estimate is reasonable.
8. When full, a 22 -gallon gas tank holds 129.8 pounds of gasoline. Estimate the weight of one gallon of gasoline. If it costs $\$ 91.30$ to fill the gas tank, estimate the cost per gallon.
9. CCGFS Use Math Tools Use estimation and mental math to find the four missing quantities from the receipt.

|  |
| :--- | :--- | :--- | :--- | :--- | :--- |



## H.O.T. Problems Higher Order Thinking

10. CCGSS Model with Mathematics Write a real-world division problem involving decimals in which you would use compatible numbers to estimate the quotient.
$\qquad$
$\qquad$
11. CCGFS Persevere with Problems Determine where to place the decimal point in the dividend and divisor so that the quotient is between 23 and 25.

$$
16023 \div 654
$$

12. CCGSS Reason Inductively Explain how you know which compatible numbers to use when estimating the quotient of a division problem involving decimals. Support your answer with an example. $\qquad$
$\qquad$
$\qquad$

## Georgia Test Practice

13. Approximately 243.0 million people live in Indonesia. The population of Germany is about 82.2 million. About how many times more people live in Indonesia than in Germany?
(A) about 2 times
(C) about 20 times
(B) about 3 times
(D) about 30 times
$\qquad$

## Extra Practice

## Estimate each quotient.

14. $54 \div 9.4 \approx$
$9 . 4 \longdiv { 5 4 } \rightarrow 9 \longdiv { 5 4 }$
15. $45.8 \div 23.6 \approx$ $\qquad$ 16. $2 3 . 3 \longdiv { 1 1 9 } \approx$
16. The average annual snowfall in King Salmon, Alaska, is 45.9 inches. The snow season lasts about 7 months of the year. About how much snow does the area receive on average each month? Explain why your answer is reasonable.
$\qquad$
$\qquad$
17. CCGFS Justify Conclusions Aurelia would like to save $\$ 474.72$ in a year to purchase a new video camera. She estimates she needs to save $\$ 40$ per month. Explain why her estimate is reasonable.
18. Scientists at the zoo recently studied an anaconda that weighs $8,643.2$ ounces. The average weight of the common rat is 11.8 ounces. About how many times heavier is the anaconda than the common rat? Explain why your answer is reasonable.
$\qquad$
$\qquad$
19. A piggy bank containing only quarters has a mass of 850 grams when empty and 7,822 grams when filled. If a quarter weighs 5.6 grams, estimate the amount of money inside the piggy bank.
20. Melanie is making homemade stickers. She uses the recipe shown to create the glue for the stickers.
a. She has 545 milliliters of vinegar. Which is a more reasonable estimate for the number of batches she can make, 5 or 7 ? Explain your answer.

Recipe: Sticker Glue

- 4 packages gelatin
- 112 milliliters vinegar
- 14 milliliters lemon extract
b. About how many times as many milliliters of vinegar are needed than lemon extract?


## Georgia Test Practice

22. The table shows the average breakdown of body weight for a 130-pound person.

| Body Part | Weight (ounces) |
| :--- | :---: |
| Water | 896 |
| Muscle | 720 |
| Skeleton | 240 |
| Head | 128 |
| Skin | 96 |

About how many times as great is the weight of water than the weight of skin?
(A) about 9
(C) about 13
(B) about 11
(D) about 15
23. Short Response For a craft activity at a day care, each child will need 1.75 yards of ribbon. If there are 25 yards of ribbon available, estimate the number of children that can participate.
24. The following advertisement was in the local newspaper.

| Bike Country |  |
| :--- | ---: |
| 26" Bike | $\$ 135.99$ |
| Folding Bike Rack | $\$ 43.95$ |
| Seat Covers | $\$ 6.59$ |
| Bike Lock | $\$ 12.89$ |
| Helmet | $\$ 29.49$ |

The cost of a $26^{\prime \prime}$ bike is equal to about how many bike locks?
(F) about 7
(H) about 9
(G) about 8
(1) about 10
25. Short Response Rewrite the following division problem using compatible numbers, so the quotient is a whole number.
$485.87 \div 71.54$

## Common Core Review

Find each quotient. мсс5.мвт. 7
26. $8.4 \div 10=$ $\qquad$
27. $1 0 0 \longdiv { 1 4 . 7 } =$ $\qquad$ 28. $94.5 \div 100=$
29. Describe the number pattern below. Then find the next three numbers. 7,345.6; 734.56; 73.456; мсс5.лвт. 2 $\qquad$ ; $\qquad$ ;
$\qquad$
30. The movie theater sold 825 tickets to fill 3 theaters. Each theater has an equal number of seats. How many seats are in each theater? mCC4.NBT. 6


## Divide Dectmals by Whole Numbers

## What You'll Learn

Scan the lesson. List two real-world scenarios in which you would divide decimals by whole numbers.

## Real-World Link

Movies Charlotte, Aaron, Maddie, and Catie went to the movies and ordered snacks from the menu shown.

1. How much did they pay for four small popcorns?

$$
\times 4=
$$

2. What is the total cost for two small packages and one large package of candy?
3. How much do four medium drinks cost?

$$
\times 4=
$$

4. What is the total cost for Exercises 1-3?

| Popcorn | $\$ \square . \square$ |
| :--- | ---: |
| Candy | $\$ \square . \square$ |
| Drinks | $+\$ \square . \square$ |
|  | $\$ \square . \square$ |

5. Estimate how much each person should pay if they split the total cost evenly.


## Divide a Decimal by a 1-Digit Number

When dividing a decimal by a whole number, divide as with whole numbers. Then place the decimal in the quotient directly above its place in the dividend.

## Example

1. Find $\mathbf{6 . 8} \div \mathbf{2}$. Estimate $6 \div 2=3$
3.4
2.8

6 ones divided by 2 is 3 ones

- 6

088 tenths divided by 2 is 4 tenths.
$-8$
$6.8 \div 2=3.4$ Compared to the estimate, the quotient is reasonable.

Got It? Do these problems to find out.
a. $7.5 \div 3$
b. $3.5 \div 7$
c. $9.8 \div 2$

## Divide a Decimal by a 2-Digit Number

## Checking Answers

To check that the answer is correct, multiply the quotient by the divisor. In Example 2,
$0.55 \times 14=7.7 . \checkmark$

The decimal point in the quotient is placed directly above its place in the dividend. In real-world situations where the division does not result in a remainder of zero, round the quotient to a specified place.

## Example

2. Find $\mathbf{7 . 7} \div \mathbf{1 4}$. Estimate $10 \div 10=1$

$7.7 \div 14=0.55$ Compared to the estimate, the quotient is reasonable.

Got It? Do these problems to find out.
d. $9.48 \div 15$
e. $3.49 \div 4$
f. $55.08 \div 17$

## Example

3. Lin is mailing a care package to his brother. The table gives the cost for mailing packages. If Lin's care package weighs 3 pounds, how much is the cost per pound?

To find the cost per pound, divide $\$ 6.74$ by 3 .

| Weight <br> (Pounds) | Cost (\$) |
| :---: | :---: |
| 1 | 4.80 |
| 2 | 5.63 |
| 3 | 6.74 |
| 4 | 7.87 |

\(\begin{array}{r}2.246 <br>
3 \longdiv { 6 . 7 4 0 } <br>

\)| -6 |
| :--- |
| 07 |
| -06 |
| 14 | <br>

$\frac{-12}{20} \\
\frac{-18}{2}\end{array}$ Annex a zero and continue dividing.
The remainder will never be zero.
Round 2.246 to 2.25 because hundredths are the smallest denomination used in money. It costs about $\$ 2.25$ per pound to mail the package.
Check Use a bar diagram and multiplication to check your work.

| 2.25 | 2.25 | 2.25 |
| :---: | :---: | :---: |

$$
\begin{aligned}
2.25 \times 3 & =6.75 \\
6.75 & \approx 6.74
\end{aligned}
$$

## Got It? Do this problem to find out.

g. Find the cost per pound of a two-pound and four-pound
 package.
g.

## Example

4. Ryan and his brother are sharing the cost of a video game. The video game costs $\mathbf{\$ 2 8 . 6 0}$. If Ryan saved $\mathbf{\$ 2 0}$ to buy the game, how much does he have left after paying his share?

| Step 1 | Determine how <br> much Ryan will pay. | Step 2 Determine how much <br> Ryan will have left. <br> 14.30 Place the decimal point. $\$ 20.00$ <br> $2 \longdiv { 2 8 . 6 0 }$  <br> -2  |
| :--- | :--- | :--- |

So, Ryan has \$5.70 left.

Got It? Do this problem to find out.
h. Kristen and her two friends are sharing the cost of a funnel cake. The funnel cake costs $\$ 5.49$. If Kristen has $\$ 2.00$, how much will she have left after she pays her share?

## Guided Practice

Divide. Round to the nearest tenth if necessary. (Examples 1 and 2 )

1. $3.6 \div 4=$
2. $12.32 \div 22=$ $\qquad$
3. $69.904 \div 34=$
4. Light travels 5.88 trillion miles in one year. How far will light travel in one month? (Examples 1 and 3 )
5. Four dozen bagels costs $\$ 30.00$. How much change will you receive if you pay for a dozen bagels with a
ten-dollar bill? (Examples 2 and 4)
6. Building on the Essential Question How can estimating quotients help you to place the decimal correctly?

## Rate Yourself!

How confident are you about dividing decimals by whole numbers? Check the box that applies.


For more help, go online to access a Personal Tutor.


FOLDABLES Time to update your Foldable!
$\qquad$

## Independent Practice

Divide. Round to the nearest tenth if necessary.
(Examples 1 and 2)

1. $39.39 \div 3=$

2. $11.4 \div 19=$ $\qquad$
3. $7.24 \div 7=$ $\qquad$
4. $55.2 \div 46=$
.   $\square$
$13118.5 \div 5=$
5. $336.752 \div 31=$
6. The Gonzalez family is taking a cruise that costs $\$ 3,082.24$ for a family of four. How much does it cost per person? (Example 3)
7. Find the average height of the buildings shown in the table. (Hint: To find the average, add the values and divide by the number of values.) (Example 4)

| World's Tallest Buildings <br> (thousands of feet) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1.667 | 1.483 | 1.483 | 1.451 | 1.381 |

19 coirs Be Precise Mr. Jamison will stain the deck in his backyard. The deck has an area of 752.4 square feet. If the deck is 33 feet long, how wide is it? Justify your procedure.
10. CCGFS Be Precise The Verrazano-Narrows Bridge in New York City is 4.26 thousand feet long and is the seventh longest suspension bridge in the world. There are 3 feet in a yard. How long is the bridge in yards? Justify your procedure.
$\qquad$
11. The Student Council is raising money by selling bottled water at a band competition. The table shows the prices for different brands. Which brand costs the least per bottle? Explain your reasoning. $\qquad$
$\qquad$
$\qquad$

## H.O.T. Problems Higher Order Thinking

12. cCGIS Persevere with Problems Find each of the following quotients. Then find a pattern and explain how you can use this pattern to mentally divide 0.0096 by 3 .
$844 \div 2 \quad 0.844 \div 2$
$84.4 \div 2$
$0.0844 \div 2$
$8.44 \div 2$
$0.00844 \div 2$
13. CCCFS Find the Error Amanda is finding $11.2 \div 14$. Find her mistake and correct it.

$\qquad$
14. CCGPS Reason Inductively Is the quotient $2.7 \div 3$
 greater than or less than 1? Explain.
15. CCGPS Use Math Tools Explain how you can use estimation to place the decimal point in the quotient $42.56 \div 22$.

## Georgia Test Practice

16. The Patterson family bought steak for a family picnic. They paid $\$ 71.94$ for 6 pounds of ribeye steak. What was the price per pound?
(A) $\$ 1.20$
(C) $\$ 10.99$
(B) $\$ 9.99$
(D) $\$ 11.99$
$\qquad$

## Extra Practice

Divide. Round to the nearest tenth if necessary.

$$
\begin{gathered}
\text { 17. } 36.8 \div 2=18.4 \\
\\
\left.\begin{array}{c}
18.4 \\
\text { mework } \\
\text { Hele }
\end{array}\right) \stackrel{-2}{36.8} \\
\\
\\
\\
\\
\\
\\
\\
\\
\\
\frac{-16}{08} \\
\frac{-8}{0}
\end{gathered}
$$

20. $10.22 \div 14=$ $\qquad$
21. $59.84 \div 32=$ $\qquad$
22. $6.271 \div 4=$
23. $751.2 \div 25=$ $\qquad$
$\qquad$
24. The Franklin Middle School jazz band plans to have a car wash to raise $\$ 468.75$ for a new sound system. In the past, they washed an average of 125 cars at each car wash. What should they charge per car so they reach their goal?
25. Marcel Park is weeding the rectangular vegetable garden. The garden has an area of 599.5 square feet. If the garden is 22 feet wide, how long is the garden? Justify your procedure.
26. CCGRS Use Math Tools The table shows the prices for different party toy packages from the Tomtown Toy Company. Which item costs the least per toy? Explain your reasoning. $\qquad$

| Cost of Party Toy Packages |  |  |
| :--- | :---: | ---: |
| Dominoes | 6-pack | $\$ 3.98$ |
| Peg Games | 12-pack | $\$ 9.99$ |
| Mini Footballs | 24-pack | $\$ 17.98$ |

## Georgia Test Practice

26. The table shows the number of subscribers to several Internet providers.

| Internet <br> Provider | Subscribers <br> (millions) |
| :---: | :---: |
| Company A | 2.45 |
| Company B | 3.12 |
| Company C | 2.83 |

If Company B earned $\$ 119$ million last month, about how much did each subscriber pay?
(A) $\$ 30$
(C) $\$ 50$
(B) $\$ 40$
(D) $\$ 60$
27. Short Response Tanner and three neighborhood friends are buying a basketball hoop that costs $\$ 249.84$. If the cost is divided equally, how much will each person pay?
28. Short Response Marvin completed 8 rounds of a trivia game and earned 94.4 points. If he earned the same number of points each round, how many points did he earn each round?

## Common Core Review

Add or subtract mentally. Use compensation. MCC5.NBT. 7
29. $0.47+0.36=$
30. $26.5-9.3=$ $\qquad$ 31. $29.4+1.7=$
32. Use $<,>$, or $=$ to compare 34.3 and 34.32. мсс5.nвт.3b
33. A king cobra has a mass of 8.845 kilograms. Round the mass to the nearest tenth kilogram. mcc5.nbt. 4
34. The same king cobra is 4.237 meters long. Round the length to the nearest meter. мсс5.мвт. 4


## Divide Decimals by Decimals

## What You'll Learn

Scan the lesson. Predict two things you will learn about dividing decimals by decimals.

## Real-World Link

Art An art studio has 36 gallons of acrylic paint. They separate it into 9 containers. How many gallons are in each container?

| Division Problem | Quotient |
| :--- | :--- |
| $36 \div 9$ |  |

Use the division problem to find patterns and complete the tables below. Then use these patterns to describe the dividends, divisors, and quotients in each set.
1.

| Division Problem | Quotient |
| :--- | :--- |
| $36 \div 0.9$ | 40 |
| $36 \div 0.09$ | 400 |
| $36 \div 0.009$ | 4,000 |
| $36 \div 0.0009$ |  |

2. 

| Division Problem | Quotient |
| :--- | :--- |
| $3.6 \div 9$ | 0.4 |
| $0.36 \div 9$ | 0.04 |
| $0.036 \div 9$ | 0.004 |
| $0.0036 \div 9$ |  |

3. 

| Division Problem | Quotient |
| :--- | :--- |
| $3.6 \div 0.9$ | 4 |
| $0.36 \div 0.09$ | 4 |
| $0.036 \div 0.009$ | 4 |
| $0.0036 \div$ | 4 |



## Essential Question

HOW can estimating be helpful?

## Common Core GPS

Content Standards MCC6.NS. 3

Mathematical Practices 1, 3, 4, 5

## Divide by Decimals

When dividing by decimals, change the divisor into a whole number. To do this, multiply both the divisor and the dividend by the same power of 10. Then divide as with whole numbers.

## Examples

1. Find $\mathbf{1 . 7 1} \div \mathbf{0 . 9}$. Estimate $2 \div 1=2$
```
Multiply by 10 to make
```

a whole number.

1.71 divided by 0.9 is 1.9. Compared to the estimate, the quotient is reasonable.

Check $1.9 \times 0.9=1.71$
2. Find $2.64 \div 0.6$.

Estimate $\square$ $\div \square$ $\square$
$0 . 6 \longdiv { 2 . 6 4 }$
Multiply 0.6 by $\square$ to make a whole number.

Multiply the dividend, $\square$ , by the same power of 10 .
a. $\qquad$
 Place the decimal point in the quotient.

Divide as with whole numbers.
2.64 divided by 0.6 is $\qquad$ Compared to the estimate, is the quotient reasonable?

## Got It? Do these problems to find out.

a. $54.4 \div 1.7$
b. $8.424 \div 0.36$
c. $0.0063 \div 0.007$

## Zeros in the Quotient and Dividend

Line up the numbers by place value as you divide. Annex zeros in the quotient in order to keep digits with the correct place value. Annex zeros in the dividend to continue dividing after the decimal point.

## Examples

3. Find $52 \div 0.4$.


So, $52 \div 0.4=130$.

Place the decimal point.

Write a zero in the ones place of the quotient because $0 \div 4=0$.

## 4. Find $0.009 \div 0.18$.



So, $0.009 \div 0.18$ is 0.05 .
5. Find $11.2 \div 0.07$.

Multiply 0.07 and 11.2 by $\qquad$ .
$0 . 0 7 \longdiv { 1 1 . 2 0 }$
Place the decimal point in the quotient.
Divide as with whole numbers.

Got It? Do these problems to find out.
d. $5.6 \div 0.014$
e. $6.24 \div 200$
f. $0.4 \div 25$

## Checking Answers

You can always check your answer to a division problem by multiplying the quotient by the divisor.

## show your

d. $\qquad$
e. $\qquad$
f. $\qquad$

## Example

6. How many times as many Internet users are there in Japan than in Spain? Round to the nearest tenth.

Find $127.4 \div 40.4$.

$$
\begin{aligned}
4 0 . 4 \longdiv { 1 2 7 . 4 } \rightarrow 4 0 4 \longdiv { 1 2 7 4 . 0 0 } \\
\frac{-1212}{620} \\
\frac{-404}{2160} \\
\frac{-2020}{140}
\end{aligned}
$$

Internet Users in 2008 (millions)

| China | $1,321.9$ |
| :--- | ---: |
| United States | 301.1 |
| Japan | 127.4 |
| France | 63.7 |
| Spain | 40.4 |
| Canada | 33.4 |

To the nearest tenth, $127.4 \div 40.4=3.2$. So, there are about 3.2 times as many Internet users in Japan than in Spain.

## Eutded Practice

Divide. (Examples 1-5)

1. $3.69 \div 0.3=$ $\qquad$ 2. $0.0338 \div 1.3=$ $\qquad$ 3. $2.943 \div 2.7=$
$\qquad$
2. Alicia bought 5.75 yards of fleece fabric to make blankets for a charity. She needs 1.85 yards of fabric for each blanket. How many blankets can Alicia make with the fabric she bought? (Example 6)
3. Building on the Essential Question When is it helpful to round the quotient to the nearest hundredth?

## Rate Yourself!

Are you ready to move on? Shade the section that applies.


For more help, go online to access a Personal Tutor.

FOLDABLES Time to update your Foldable!

## Independent Practics

Divide. (Examples 1-5)

1. $1.44 \div 0.4=$

2. $96.6 \div 0.42=$ $\qquad$ 5. $13.5 \div 0.03=$ $\qquad$ 6. $0.12 \div 0.15=$ $\qquad$
3. CCGSS Use Math Tools The average person's stride length, the distance covered by one step, is approximately 2.5 feet long. How many steps would the average person take to travel 50 feet? (Example 6)
4. SiIn Alaska has a coastline of about 6.64 thousand miles. Florida has about 1.35 thousand miles of coastline. How many times more coastline does Alaska have than Florida? Round to the nearest tenth if necessary. Justify your procedure.
5. CCGFS Model with Mathematics Refer to the graphic novel frame below for Exercises a-b.

a. How many hours does Raj need to work to earn the remainder of the money he needs to buy the video game system?
b. Suppose Raj receives a raise for his hard work and now earns $\$ 6.25$ per hour. How many hours would he need to work to earn $\$ 132$ ?
6. A necklace is being made with beads that are 1.25 centimeters in diameter each. The necklace is 30 centimeters long. How many beads are needed? $\qquad$

11 cCGFS Use Math Tools Use the table that shows popular sports car colors in North America.
a. How many times more respondents chose silver than red? Round to the nearest tenth if necessary.
b. How many times more respondents chose either silver or black than red? Round to the nearest tenth if necessary.

| Popular Sports Car Colors |  |
| :--- | :---: |
| Color | Portion of Responses |
| Silver | 0.2 |
| Blue | 0.16 |
| Black | 0.14 |
| Red | 0.09 |
| Other | 0.41 |

## H.O.T. Problems Higher Order Thinking

12. CCGFS Persevere with Problems Find two positive decimals $a$ and $b$ that make the following statement true. Then find two positive decimals $a$ and $b$ that make the statement false.

$$
\text { If } a<1 \text { and } b<1 \text {, then } a \div b<1
$$

13. CCGFS Which One Doesn't Belong? Identify the problem that does not have the same quotient as the other three. Explain your reasoning.
$49 \div 7 \quad 4.9 \div 7 \quad 0.49 \div 0.7 \quad 0.049 \div 0.07$

## Georgia Test Practice

14. To the nearest tenth, how many times as many people in the U.S. own dogs as own birds?
(A) 6.8
(B) 12.2
(C) 26.6
(D) 35.8

$\qquad$

## ExtraPractice

## Divide.

16. $2.07 \div 0.9=$
17. $8.4 \div 0.02=$ $\qquad$ 20. $0.242 \div 0.4=$ $\qquad$
18. CCGPS Use Math Tools Find examples of decimals in a newspaper or magazine. Write a real-world problem in which you would divide decimals.
19. A submarine sandwich 1.5 feet long is cut into 0.25 -foot pieces. How many pieces will there be?
20. The table shows the five most populated countries in the world. How many times as many people live in China than in the United States? Round to the nearest tenth if necessary.

| Most Populated Countries |  |
| :--- | :---: |
| Country | Approximate <br> Population (billions) |
| China | 1.325 |
| India | 1.13 |
| United States | 0.304 |
| Indonesia | 0.235 |
| Brazil | 0.19 |

24. CCGRS Justify Conclusions Lake Superior, along the U.S.-Canadian border, has a maximum depth of 1.333 thousand feet. There are 5,280 feet in one mile. How deep is Lake Superior in miles? Round to the nearest hundredth if necessary. Explain your answer.


## Georgia Test Practice

25. Ava paid $\$ 4.90$ for 2.5 pounds of walnuts. What is the cost of one pound of walnuts?
(A) $\$ 0.96$
(B) $\$ 1.76$
(C) $\$ 1.86$
(D) $\$ 1.96$
26. Short Response Max bicycled 6.25 miles in 30.5 minutes. On average, how far did he bicycle each minute? Round to the nearest tenth.
27. The table shows the approximate number of people in the world who speak either Spanish or French.

| Language | Speakers (billions) |
| :--- | :---: |
| Spanish | 0.425 |
| French | 0.129 |

To the nearest tenth, how many times as many people speak Spanish as French?
(F) 0.2
(H) 0.3
(G) 1.1
(1) 3.3
28. Short Response About 24.8 million people live in Texas. About 0.6 million people live in Vermont. How many times as many people live in Texas than in Vermont? Round to the nearest tenth if necessary.

## CCARS Common Core Review

Fill in each $\square$ with $<,>$, or $=$ to make a true sentence. MCC4.NF. 2
29. $\frac{2}{4} \bigcirc \frac{5}{8}$
30. $\frac{6}{12} \bigcirc \frac{5}{10}$
31. $\frac{1}{2} \bigcirc \frac{6}{14}$
32. Plot the fraction $\frac{7}{12}$ on the number line. Is $\frac{7}{12}$ closer to $0, \frac{1}{2}$, or 1 ? MCC4.NF. 2

33. Lily spent $\frac{1}{6}$ of her free time practicing soccer and $\frac{5}{12}$ of her free time playing a video game. What fraction of her free time did she spend on these two activities? mcc5.NF. 2


##  <br> SENTUBYY CARED

## in Design

## Sports Equipment Designer

Do you have a passion for sports and a strong interest in science? Are you a creative thinker who always has new ideas or better ways of doing things? If so, then you should consider a career designing sports equipment. Sports equipment designers combine creativity and engineering principles to create equipment that is cutting edge and helps improve athletic performance. They design everything from baseball bats and footballs to lacrosse protective gear and racing wheelchairs.

## Gaining a Competitive Edge

When a punter kicks a football, the ball has both horizontal motion and vertical motion. The table shows these values when a football is kicked at 25 meters per second.
Use the information in the table to solve each problem. Assume that each football is kicked at 25 meters per second. Round to the nearest tenth if necessary.

1. The hang time, or time that a football is in the air, of a football that is kicked at a $27^{\circ}$ angle is given by $0.204 \times 11.3$. What is the approximate hang time?
2. How much greater is the hang time of a football that is kicked at a $62^{\circ}$ angle than one that is kicked at a $45^{\circ}$ angle? Use the expressions $0.204 \times 22.1$ and $0.204 \times 17.7$.
3. The final distance from the punter to a football kicked at a $27^{\circ}$ angle is approximately $22.3 \times 11.3 \times 0.2$. What is the distance from the punter to the football?

| Punting A Football |  |  |
| :---: | :---: | :---: |
| Angle <br> of Kick | Horizontal <br> Motion (m/s) | Vertical <br> Motion $(\mathbf{m} / \mathbf{s})$ |
| $27^{\circ}$ | 22.3 | 11.3 |
| $45^{\circ}$ | 17.7 | 17.7 |
| $62^{\circ}$ | 11.7 | 22.1 |

4. Find the distance of a football that is kicked at an angle of $62^{\circ}$ if the distance is found by using the expression
$11.7 \times 22.1 \times 0.2$.
5. The hang time of a football is about 3 seconds. Find $3 \div 0.204$ to determine the vertical motion of the football.
6. A football reaches its maximum height in $y \div 9.8$ seconds. A football is kicked at a $62^{\circ}$ angle. At the same time, another football is kicked at a $27^{\circ}$ angle. Which reaches its maximum height first? Explain.


## Career Project

It's time to update your career portfolio! Choose a piece of sports equipment and describe how it has changed over the past 20 years. List the reasons for the changes.

Suppose you are an employer hiring a sports equipment designer. What questions would you ask a potential employee?
-
-
-

## Vocabulary Check

Write the correct term for each clue in the crossword puzzle.


## Across

1. easy to divide mentally
2. a number that has a digit in the tenths place, hundredths place, or beyond
3. to find an approximate value for a number

## Down

2. the answer to a multiplication problem
3. a number with more than one digit
4. the number by which the dividend is being divided
5. a number that is being divided

## Key Concept Check

## Use Your Foldables

Use your Foldable to help review the chapter.

## Divide with Decimals

Examples
Examples

## Got it?

Complete the cross number puzzle by solving the problems.


Across

1. $34.5 \times 14$
2. $569.6 \div 3.2$
3. $18.5 \times 40$
4. $50.4 \div 2.4$
5. $562.39+304.61$
6. $42.5 \times 116$
7. $339.2 \times 2.5$
8. $1,584 \div 4.5$
9. $1,218 \div 6$

Down

1. $24.3+15.7$
2. $21.2 \times 17.5$
3. $33.75 \times 3.2$
4. $146.53+92.47$
5. $2,628 \div 36.5$
6. $24 \times 4.5$
7. $263.4+199.6$
8. $35.2 \times 25$

## Problem Solving

1. A car travels 57.9 miles per hour for 3.2 hours. Estimate the number of miles driven. (Lesson 1)
2. A loaf of bread costs $\$ 1.79$. How much would five loaves cost? (Lesson 3)
$\qquad$
$\qquad$
3. What is the area of the base of the fountain below? (Lesson 4) $\qquad$

4. A marathon race is 26.2 miles long. Lacey ran the marathon in 3.6 hours. On average, how many miles did she run per hour? Round to the nearest tenth. (Lesson 8)
$\qquad$
5. The speed of light is $1.86 \times 100,000$ miles per second. Write this number in standard form. (Lesson 4) $\qquad$
$\qquad$
6. How many dimes are in $\$ 8,590$ ? (Lesson 7)
7. cCCRS Use Math Tools The table shows the height of members of Evan's family. His sister, Cindy, is 0.8 times his height. Which is a reasonable height for Cindy: about 4 feet, 4.5 feet, or 6 feet?
Explain. (Lesson 4)

| Family Member | Height (ft) |
| :--- | :---: |
| Evan | 5.75 |
| Grace | 5.5 |
| Jasper | 6.25 |
| Tron | 5.25 |

## Reflect

## Answering the Essential Question

Use what you learned about computing with multi-digit numbers to complete the graphic organizer.

(3)

Answer the Essential Question. HOW can estimating be helpful?

